

ИДЗ 1 Дифференциальные уравнения высших порядков

Задача 1. Найти общее решение дифференциального уравнения.

$$1.1. y'''x \ln x = y''.$$

$$1.3. 2xy''' = y''.$$

$$1.5. \operatorname{tg} x \cdot y'' - y' + \frac{1}{\sin x} = 0.$$

$$1.7. y''' \operatorname{ctg} 2x + 2y'' = 0.$$

$$1.9. \operatorname{tg} x \cdot y''' = 2y''.$$

$$1.11. x^4 y'' + x^3 y' = 1.$$

$$1.13. (1+x^2) y'' + 2xy' = x^3.$$

$$1.15. xy''' - y'' + \frac{1}{x} = 0.$$

$$1.17. \operatorname{th} x \cdot y^{IV} = y'''.$$

$$1.19. y'' \operatorname{tg} x = y'' + 1.$$

$$1.21. y''' \operatorname{th} 7x = 7y''.$$

$$1.23. \operatorname{cth} x \cdot y'' - y' + \frac{1}{\operatorname{ch} x} = 0.$$

$$1.25. (1+\sin x) y''' = \cos x \cdot y''.$$

$$1.27. -xy''' + 2y'' = \frac{2}{x^2}.$$

$$1.29. x^4 y'' + x^3 y' = 4.$$

$$1.31. (1+x^2) y'' + 2xy' = 12x^3.$$

$$1.33. 2xy''' = y''.$$

$$1.35. xy''' - y'' + \frac{1}{x} = 0.$$

$$1.37. -xy''' + 2y'' = \frac{2}{x^2}.$$

$$1.39. \operatorname{tg} x \cdot y''' = 2y''.$$

$$1.2. xy''' + y'' = 1.$$

$$1.4. xy''' + y'' = x + 1.$$

$$1.6. x^2 y'' + xy' = 1.$$

$$1.8. x^3 y''' + x^2 y'' = 1.$$

$$1.10. y''' \operatorname{cth} 2x = 2y''.$$

$$1.12. xy''' + 2y'' = 0.$$

$$1.14. x^5 y''' + x^4 y'' = 1.$$

$$1.16. xy''' + y'' + x = 0.$$

$$1.18. xy''' + y'' = \sqrt{x}.$$

$$1.20. y''' \operatorname{tg} 5x = 5y''.$$

$$1.22. x^3 y''' + x^2 y'' = \sqrt{x}.$$

$$1.24. (x+1) y''' + y'' = (x+1).$$

$$1.26. xy''' + y'' = \frac{1}{\sqrt{x}}.$$

$$1.28. \operatorname{cth} xy'' + y' = \operatorname{ch} x.$$

$$1.30. y'' + \frac{2x}{x^2 + 1} y' = 2x.$$

$$1.32. xy''' + 2y'' = 0.$$

$$1.34. (x+1) y''' + y'' = (x+1).$$

$$1.36. x^2 y'' + xy' = 1.$$

$$1.38. xy''' + y'' = \sqrt{x}.$$

$$1.40. y'' + \frac{2x}{x^2 + 1} y' = 2x.$$

Задача 2. Найти решение задачи Коши.

$$2.1. 4y^3 y'' = y^4 - 1, \quad y(0) = \sqrt{2}, \quad y'(0) = 1/(2\sqrt{2}).$$

$$2.2. y'' = 128y^3, \quad y(0) = 1, \quad y'(0) = 8.$$

$$2.3. y''y^3 + 64 = 0, \quad y(0) = 4, \quad y'(0) = 2.$$

$$2.4. \quad y'' + 2\sin y \cos^3 y = 0, \quad y(0) = 0, \quad y'(0) = 1.$$

$$2.5. \quad y'' = 32\sin^3 y \cos y, \quad y(1) = \pi/2, \quad y'(1) = 4.$$

$$2.6. \quad y'' = 98y^3, \quad y(1) = 1, \quad y'(1) = 7.$$

$$2.7. \quad y''y^3 + 49 = 0, \quad y(3) = -7, \quad y'(3) = -1.$$

$$2.8. \quad 4y^3y'' = 16y^4 - 1, \quad y(0) = \sqrt{2}/2, \quad y'(0) = 1/\sqrt{2}.$$

$$2.9. \quad y'' + 8\sin y \cos^3 y = 0, \quad y(0) = 0, \quad y'(0) = 2.$$

$$2.10. \quad y'' = 72y^3, \quad y(2) = 1, \quad y'(2) = 6.$$

$$2.11. \quad y''y^3 + 36 = 0, \quad y(0) = 3, \quad y'(0) = 2.$$

$$2.12. \quad y'' = 18\sin^3 y \cos y, \quad y(1) = \pi/2, \quad y'(1) = 3.$$

$$2.13. \quad 4y^3y'' = y^4 - 16, \quad y(0) = 2\sqrt{2}, \quad y'(0) = 1/\sqrt{2}.$$

$$2.14. \quad y'' = 50y^3, \quad y(3) = 1, \quad y'(3) = 5.$$

$$2.15. \quad y''y^3 + 25 = 0, \quad y(2) = -5, \quad y'(2) = -1.$$

$$2.16. \quad y'' + 18\sin y \cos^3 y = 0, \quad y(0) = 0, \quad y'(0) = 3.$$

$$2.17. \quad y'' = 8\sin^3 y \cos y, \quad y(1) = \pi/2, \quad y'(1) = 2.$$

$$2.18. \quad y'' = 32y^3, \quad y(4) = 1, \quad y'(4) = 4.$$

$$2.19. \quad y''y^3 + 16 = 0, \quad y(1) = 2, \quad y'(1) = 2.$$

$$2.20. \quad y'' + 32\sin y \cos^3 y = 0, \quad y(0) = 0, \quad y'(0) = 4.$$

$$2.21. \quad y'' = 50\sin^3 y \cos y, \quad y(1) = \pi/2, \quad y'(1) = 5.$$

$$2.22. \quad y'' = 18y^3, \quad y(1) = 1, \quad y'(1) = 3.$$

$$2.23. \quad y''y^3 + 9 = 0, \quad y(1) = 1, \quad y'(1) = 3.$$

$$2.24. \quad y^3y'' = 4(y^4 - 1), \quad y(0) = \sqrt{2}, \quad y'(0) = \sqrt{2}.$$

$$2.25. \quad y'' + 50\sin y \cos^3 y = 0, \quad y(0) = 0, \quad y'(0) = 5.$$

$$2.26. \quad y'' = 8y^3, \quad y(0) = 1, \quad y'(0) = 2.$$

$$2.27. \quad y''y^3 + 4 = 0, \quad y(0) = -1, \quad y'(0) = -2.$$

$$2.28. \quad y'' = 2\sin^3 y \cos y, \quad y(1) = \pi/2, \quad y'(1) = 1.$$

$$2.29. \quad y^3y'' = y^4 - 16, \quad y(0) = 2\sqrt{2}, \quad y'(0) = \sqrt{2}.$$

$$2.30. \quad y'' = 2y^3, \quad y(-1) = 1, \quad y'(-1) = 1.$$

$$2.31. \quad y''y^3 + 1 = 0, \quad y(1) = -1, \quad y'(1) = -1.$$

$$2.32. \quad y'' = 18\sin^3 y \cos y, \quad y(1) = \pi/2, \quad y'(1) = 3.$$

$$2.33. \quad y''y^3 + 64 = 0, \quad y(0) = 4, \quad y'(0) = 2.$$

$$2.34. y^3 y'' = 4(y^4 - 1), \quad y(0) = \sqrt{2}, \quad y'(0) = \sqrt{2}.$$

$$2.35. y'' y^3 + 25 = 0, \quad y(2) = -5, \quad y'(2) = -1.$$

$$2.36. y'' = 98y^3, \quad y(1) = 1, \quad y'(1) = 7.$$

$$2.37. y'' y^3 + 4 = 0, \quad y(0) = -1, \quad y'(0) = -2.$$

$$2.38. y'' = 32y^3, \quad y(4) = 1, \quad y'(4) = 4.$$

$$2.39. y'' + 8 \sin y \cos^3 y = 0, \quad y(0) = 0, \quad y'(0) = 2.$$

$$2.40. y'' = 2y^3, \quad y(-1) = 1, \quad y'(-1) = 1.$$

Задача 3. Найти общее решение дифференциального уравнения.

$$3.1. y''' + 3y'' + 2y' = 1 - x^2.$$

$$3.3. y''' - y' = x^2 + x.$$

$$3.5. y^{IV} - y''' = 5(x+2)^2.$$

$$3.7. y^{IV} + 2y''' + y'' = x^2 + x - 1.$$

$$3.9. 3y^{IV} + y''' = 6x - 1.$$

$$3.11. y''' + y'' = 5x^2 - 1.$$

$$3.13. 7y''' - y'' = 12x.$$

$$3.15. y''' - y' = 3x^2 - 2x + 1.$$

$$3.17. y^{IV} - 3y''' + 3y'' - y' = x - 3.$$

$$3.19. y''' - 4y'' = 32 - 384x^2.$$

$$3.21. y''' + y'' = 49 - 24x^2.$$

$$3.23. y''' - 13y'' + 12y' = x - 1.$$

$$3.25. y''' - y'' = 6x + 5.$$

$$3.27. y''' - 5y'' + 6y' = (x-1)^2.$$

$$3.29. y''' - 13y'' + 12y' = 18x^2 - 39.$$

$$3.31. y''' - 5y'' + 6y' = 6x^2 + 2x - 5.$$

$$3.33. y''' - y' = x^2 + x.$$

$$3.35. y''' - y' = 3x^2 - 2x + 1.$$

$$3.37. y''' - 5y'' + 6y' = (x-1)^2.$$

$$3.39. 3y^{IV} + y''' = 6x - 1.$$

$$3.2. y''' - y'' = 6x^2 + 3x.$$

$$3.4. y^{IV} - 3y''' + 3y'' - y' = 2x.$$

$$3.6. y^{IV} - 2y''' + y'' = 2x(1-x).$$

$$3.8. y^V - y^{IV} = 2x + 3.$$

$$3.10. y^{IV} + 2y''' + y'' = 4x^2.$$

$$3.12. y^{IV} + 4y''' + 4y'' = x - x^2.$$

$$3.14. y''' + 3y'' + 2y' = 3x^2 + 2x.$$

$$3.16. y''' - y'' = 4x^2 - 3x + 2.$$

$$3.18. y^{IV} + 2y''' + y'' = 12x^2 - 6x.$$

$$3.20. y^{IV} + 2y''' + y'' = 2 - 3x^2.$$

$$3.22. y''' - 2y'' = 3x^2 + x - 4.$$

$$3.24. y^{IV} + y''' = x.$$

$$3.26. y''' + 3y'' + 2y' = x^2 + 2x + 3.$$

$$3.28. y^{IV} - 6y''' + 9y'' = 3x - 1.$$

$$3.30. y^{IV} + y''' = 12x + 6.$$

$$3.32. y^{IV} + 4y''' + 4y'' = x - x^2.$$

$$3.34. y^{IV} + y''' = x.$$

$$3.36. y^{IV} - 2y''' + y'' = 2x(1-x).$$

$$3.38. y^{IV} + 2y''' + y'' = 12x^2 - 6x.$$

$$3.40. y^{IV} + y''' = 12x + 6.$$

Задача 4. Найти общее решение дифференциального уравнения.

$$4.1. y''' - 4y'' + 5y' - 2y = (16 - 12x)e^{-x}.$$

$$4.2. y''' - 3y'' + 2y' = (1 - 2x)e^x.$$

$$4.3. y''' - y'' - y' + y = (3x + 7)e^{2x}.$$

$$4.4. y''' - 2y'' + y' = (2x+5)e^{2x}.$$

$$4.5. y''' - 3y'' + 4y = (18x-21)e^{-x}.$$

$$4.6. y''' - 5y'' + 8y' - 4y = (2x-5)e^x.$$

$$4.7. y''' - 4y'' + 4y' = (x-1)e^x.$$

$$4.8. y''' + 2y'' + y' = (18x+21)e^{2x}.$$

$$4.9. y''' + y'' - y' - y = (8x+4)e^x.$$

$$4.10. y''' - 3y' - 2y = -4x \cdot e^x.$$

$$4.11. y''' - 3y' + 2y = (4x+9)e^{2x}.$$

$$4.12. y''' + 4y'' + 5y' + 2y = (12x+16)e^x.$$

$$4.13. y''' - y'' - 2y' = (6x-11)e^{-x}.$$

$$4.14. y''' + y'' - 2y' = (6x+5)e^x.$$

$$4.15. y''' + 4y'' + 4y' = (9x+15)e^x.$$

$$4.16. y''' - 3y'' - y' + 3y = (4-8x)e^x.$$

$$4.17. y''' - y'' - 4y' + 4y = (7-6x)e^x.$$

$$4.18. y''' + 3y'' + 2y' = (1-2x)e^{-x}.$$

$$4.19. y''' - 5y'' + 7y' - 3y = (20-16x)e^{-x}.$$

$$4.20. y''' - 4y'' + 3y' = -4x \cdot e^x.$$

$$4.21. y''' - 5y'' + 3y' + 9y = (32x-32)e^{-x}.$$

$$4.22. y''' - 6y'' + 9y' = 4x \cdot e^x.$$

$$4.23. y''' - 7y'' + 15y' - 9y = (8x-12)e^x.$$

$$4.24. y''' - y'' - 5y' - 3y = -(8x+4)e^x.$$

$$4.25. y''' + 5y'' + 7y' + 3y = (16x+20)e^x.$$

$$4.26. y''' - 2y'' - 3y' = (8x-14)e^{-x}.$$

$$4.27. y''' + 2y'' - 3y' = (8x+6)e^x.$$

$$4.28. y''' + 6y'' + 9y' = (16x+24)e^x.$$

$$4.29. y''' - y'' - 9y' + 9y = (12-16x)e^x.$$

$$4.30. y''' + 4y'' + 3y' = 4(1-x)e^{-x}.$$

$$4.31. y''' + y'' - 6y' = (20x+14)e^{2x}.$$

$$4.32. y''' + 4y'' + 5y' + 2y = (12x+16)e^x.$$

$$4.33. y''' - y'' - y' + y = (3x+7)e^{2x}.$$

$$4.34. y''' - y'' - 5y' - 3y = -(8x + 4)e^x.$$

$$4.35. y''' + 4y'' + 4y' = (9x + 15)e^x.$$

$$4.36. y''' - 5y'' + 8y' - 4y = (2x - 5)e^x.$$

$$4.37. y''' + 2y'' - 3y' = (8x + 6)e^x.$$

$$4.38. y''' + 3y'' + 2y' = (1 - 2x)e^{-x}.$$

$$4.39. y''' + y'' - y' - y = (8x + 4)e^x.$$

$$4.40. y''' + 4y'' + 3y' = 4(1 - x)e^{-x}.$$

Задача 5. Найти общее решение дифференциального уравнения.

$$5.1. y'' + 2y' = 4e^x (\sin x + \cos x).$$

$$5.2. y'' - 4y' + 4y = -e^{2x} \sin 6x.$$

$$5.3. y'' + 2y' = -2e^x (\sin x + \cos x).$$

$$5.4. y'' + y = 2\cos 7x + 3\sin 7x.$$

$$5.5. y'' + 2y' + 5y = -\sin 2x.$$

$$5.6. y'' - 4y' + 8y = e^x (5\sin x - 3\cos x).$$

$$5.7. y'' + 2y' = e^x (\sin x + \cos x).$$

$$5.8. y'' - 4y' + 4y = e^{2x} \sin 3x.$$

$$5.9. y'' + 6y' + 13y = e^{-3x} \cos 4x.$$

$$5.10. y'' + y = 2\cos 3x - 3\sin 3x.$$

$$5.11. y'' + 2y' + 5y = -2\sin x.$$

$$5.12. y'' - 4y' + 8y = e^x (-3\sin x + 4\cos x).$$

$$5.13. y'' + 2y' = 10e^x (\sin x + \cos x).$$

$$5.14. y'' - 4y' + 4y = e^{2x} \sin 5x.$$

$$5.15. y'' + y = 2\cos 5x + 3\sin 5x.$$

$$5.16. y'' + 2y' + 5y = -17\sin 2x.$$

$$5.17. y'' + 6y' + 13y = e^{-3x} \cos x.$$

$$5.18. y'' - 4y' + 8y = e^x (3\sin x + 5\cos x).$$

$$5.19. y'' + 2y' = 6e^x (\sin x + \cos x).$$

$$5.20. y'' - 4y' + 4y = -e^{2x} \sin 4x.$$

$$5.21. y'' + 6y' + 13y = -e^{3x} \cos 5x.$$

$$5.22. y'' + y = 2\cos 7x - 3\sin 7x.$$

$$5.23. y'' + 2y' + 5y = -\cos x.$$

$$5.24. y'' - 4y' + 8y = e^x (2\sin x - \cos x).$$

$$5.25. y'' + 2y' = 3e^x (\sin x + \cos x).$$

$$5.26. y'' - 4y' + 4y = e^{2x} \sin 4x.$$

$$5.27. y'' + 6y' + 13y = e^{-3x} \cos 8x.$$

$$5.28. y'' + 2y' + 5y = 10\cos x.$$

$$5.29. y'' + y = 2\cos 4x + 3\sin 4x.$$

$$5.30. y'' - 4y' + 8y = e^x (-\sin x + 2\cos x).$$

$$5.31. y'' - 4y' + 4y = e^{2x} \sin 6x.$$

$$5.32. y'' - 4y' + 8y = e^x (-3\sin x + 4\cos x).$$

$$5.33. y'' + 2y' = -2e^x (\sin x + \cos x).$$

$$5.34. y'' - 4y' + 8y = e^x (2\sin x - \cos x).$$

$$5.35. y'' + y = 2\cos 5x + 3\sin 5x.$$

$$5.36. y'' - 4y' + 8y = e^x (5\sin x - 3\cos x).$$

$$5.37. y'' + 6y' + 13y = e^{-3x} \cos 8x.$$

$$5.38. y'' - 4y' + 8y = e^x (3\sin x + 5\cos x).$$

$$5.39. y'' + 6y' + 13y = e^{-3x} \cos 4x.$$

$$5.40. y'' - 4y' + 8y = e^x (-\sin x + 2\cos x).$$

Задача 6. Найти общее решение дифференциального уравнения.

$$6.1. y'' - 2y' = 2\operatorname{ch} 2x.$$

$$6.2. y'' + y = 2\sin x - 6\cos x + 2e^x.$$

$$6.3. y''' - y' = 2e^x + \cos x.$$

$$6.4. y'' - 3y' = 2\operatorname{ch} 3x.$$

$$6.5. y'' + 4y = -8\sin 2x + 32\cos 2x + 4e^{2x}.$$

$$6.6. y''' - y' = 10\sin x + 6\cos x + 4e^x.$$

- 6.7. $y'' - 4y' = 16\operatorname{ch} 4y.$
- 6.9. $y''' - 4y' = 24e^{2x} - 4\cos 2x + 8\sin 2x.$
- 6.11. $y'' + 16y = 16\cos 4x - 16e^{4x}.$
- 6.13. $y'' - y' = 2\operatorname{ch} x.$
- 6.15. $y''' - 16y' = 48e^{4x} + 64\cos 4x - 64\sin 4x.$
- 6.17. $y'' + 36y = 24\sin 6x - 12\cos 6x + 36e^{6x}.$
- 6.19. $y'' + 3y' = 2\operatorname{sh} 3x.$
- 6.21. $y''' - 36y' = 36e^{6x} - 72(\cos 6x + \sin 6x).$
- 6.23. $y'' + 64y = 16\sin 8x - 16\cos 8x - 64e^{8x}.$
- 6.25. $y'' + 5y' = 50\operatorname{sh} 5x.$
- 6.27. $y''' - 64y' = 128\cos 8x - 64e^{8x}.$
- 6.29. $y'' + 100y = 20\sin 10x - 30\cos 10x - 200e^{10x}.$
- 6.31. $y''' - 100y' = 20e^{10x} + 100\cos 10x.$
- 6.33. $y''' - y' = 2e^x + \cos x.$
- 6.35. $y''' - 16y' = 48e^{4x} + 64\cos 4x - 64\sin 4x.$
- 6.37. $y''' - 64y' = 128\cos 8x - 64e^{8x}.$
- 6.39. $y''' - 4y' = 24e^{2x} - 4\cos 2x + 8\sin 2x.$
- 6.8. $y'' + 9y = -18\sin 3x - 18e^{3x}.$
- 6.10. $y'' - 5y' = 50\operatorname{ch} 5x.$
- 6.12. $y''' - 9y' = -9e^{3x} + 18\sin 3x - 9\cos 3x.$
- 6.14. $y'' + 25y = 20\cos 5x - 10\sin 5x + 50e^{5x}.$
- 6.16. $y'' + 2y' = 2\operatorname{sh} 2x.$
- 6.18. $y''' - 25y' = 25(\sin 5x + \cos 5x) - 50e^{5x}.$
- 6.20. $y'' + 49y = 14\sin 7x + 7\cos 7x - 98e^{7x}.$
- 6.22. $y'' + 4y' = 16\operatorname{sh} 4x.$
- 6.24. $y''' - 49y' = 14e^{7x} - 49(\cos 7x + \sin 7x).$
- 6.26. $y'' + 81y = 9\sin 9x + 3\cos 9x + 162e^{9x}.$
- 6.28. $y'' + y' = 2\operatorname{sh} x.$
- 6.30. $y''' - 81y' = 162e^{9x} + 81\sin 9x.$
- 6.32. $y''' - 9y' = -9e^{3x} + 18\sin 3x - 9\cos 3x.$
- 6.34. $y''' - 49y' = 14e^{7x} - 49(\cos 7x + \sin 7x).$
- 6.36. $y''' - y' = 10\sin x + 6\cos x + 4e^x.$
- 6.38. $y''' - 25y' = 25(\sin 5x + \cos 5x) - 50e^{5x}.$
- 6.40. $y''' - 81y' = 162e^{9x} + 81\sin 9x.$

Задача 7. Найти численное решение задачи Коши, сравнить его с аналитическим.

- 7.1. $y'' + \pi^2 y = \pi^2 / \cos \pi x, \quad y(0) = 3, \quad y'(0) = 0.$
- 7.2. $y'' + 3y' = 9e^{3x} / (1 + e^{3x}), \quad y(0) = \ln 4, \quad y'(0) = 3(1 - \ln 2).$
- 7.3. $y'' + 4y = 8\operatorname{ctg} 2x, \quad y(\pi/4) = 5, \quad y'(\pi/4) = 4.$
- 7.4. $y'' - 6y' + 8y = 4 / (1 + e^{-2x}), \quad y(0) = 1 + 2\ln 2, \quad y'(0) = 6\ln 2.$
- 7.5. $y'' - 9y' + 18y = 9e^{3x} / (1 + e^{-3x}), \quad y(0) = 0, \quad y'(0) = 0.$
- 7.6. $y'' + \pi^2 y = \pi^2 / \sin \pi x = 1, \quad y(1/2), \quad y'(1/2) = \pi^2 / 2.$
- 7.7. $y'' + \frac{1}{\pi^2} y = \frac{1}{\pi^2 \cos(x/\pi)}, \quad y(0) = 2, \quad y'(0) = 0.$
- 7.8. $y'' - 3y' = \frac{9e^{-3x}}{3 + e^{-3x}}, \quad y(0) = 4\ln 4, \quad y'(0) = 3(3\ln 4 - 1).$
- 7.9. $y'' + y = 4\operatorname{ctg} x, \quad y(\pi/2) = 4, \quad y'(\pi/2) = 4.$
- 7.10. $y'' - 6y' + 8y = 4 / (2 + e^{-2x}), \quad y(0) = 1 + 3\ln 3, \quad y'(0) = 10\ln 3.$
- 7.11. $y'' + 6y' + 8y = 4e^{-2x} / (2 + e^{2x}), \quad y(0) = 0, \quad y'(0) = 0.$
- 7.12. $y'' + 9y = 9 / \sin 3x, \quad y(\pi/6) = 4, \quad y'(\pi/6) = 3\pi/2.$

$$7.13. y'' + 9y = 9/\cos 3x, \quad y(0) = 1, \quad y'(0) = 0.$$

$$7.14. y'' - y' = e^{-x}/(2 + e^{-x}), \quad y(0) = \ln 27, \quad y'(0) = \ln 9 - 1.$$

$$7.15. y'' + 4y = 4\operatorname{ctg} 2x, \quad y(\pi/4) = 3, \quad y'(\pi/4) = 2.$$

$$7.16. y'' - 3y' + 2y = \frac{1}{3 + e^{-x}}, \quad y(0) = 1 + 8\ln 2, \quad y'(0) = 14\ln 2.$$

$$7.17. y'' - 6y' + 8y = 4e^{2x}/(1 + e^{-2x}), \quad y(0) = 0, \quad y'(0) = 0.$$

$$7.18. y'' + 16y = 16/\sin 4x, \quad y(\pi/8) = 3, \quad y'(\pi/8) = 2\pi.$$

$$7.19. y'' + 16y = 16/\cos 4x, \quad y(0) = 3, \quad y'(0) = 0.$$

$$7.20. y'' - 2y' = 4e^{-2x}/(1 + e^{-2x}), \quad y(0) = \ln 4, \quad y'(0) = \ln 4 - 2.$$

$$7.21. y'' + \frac{y}{4} = \frac{1}{4} \operatorname{ctg}(x/2), \quad y(\pi) = 2, \quad y'(\pi) = 1/2.$$

$$7.22. y'' - 3y' + 2y = 1/(2 + e^{-x}), \quad y(0) = 1 + 3\ln 3, \quad y'(0) = 5\ln 3.$$

$$7.23. y'' + 3y' + 2y = e^{-x}/(2 + e^x), \quad y(0) = 0, \quad y'(0) = 0.$$

$$7.24. y'' + 4y = 4/\sin 2x, \quad y(\pi/4) = 2, \quad y'(\pi/4) = \pi.$$

$$7.25. y'' + 4y = 4/\cos 2x, \quad y(0) = 2, \quad y'(0) = 0.$$

$$7.26. y'' + y' = e^x/(2 + e^x), \quad y(0) = \ln 27, \quad y'(0) = 1 - \ln 9.$$

$$7.27. y'' + y = 2\operatorname{ctg} x, \quad y(\pi/2) = 1, \quad y'(\pi/2) = 2.$$

$$7.28. y'' - 3y' + 2y = 1/(1 + e^{-x}), \quad y(0) = 1 + 2\ln 2, \quad y'(0) = 3\ln 2.$$

$$7.29. y'' - 3y' + 2y = e^x/(1 + e^{-x}), \quad y(0) = 0, \quad y'(0) = 0.$$

$$7.30. y'' + y = 1/\sin x, \quad y(\pi/2) = 1, \quad y'(\pi/2) = \pi/2.$$

$$7.31. y'' + y = 1/\cos x, \quad y(0) = 1, \quad y'(0) = 0.$$

$$7.32. y'' + 9y = 9/\sin 3x, \quad y(\pi/6) = 4, \quad y'(\pi/6) = 3\pi/2.$$

$$7.33. y'' + 4y = 8\operatorname{ctg} 2x, \quad y(\pi/4) = 5, \quad y'(\pi/4) = 4.$$

$$7.34. y'' + 4y = 4/\sin 2x, \quad y(\pi/4) = 2, \quad y'(\pi/4) = \pi.$$

$$7.35. y'' + 4y = 4\operatorname{ctg} 2x, \quad y(\pi/4) = 3, \quad y'(\pi/4) = 2.$$

$$7.36. y'' + \pi^2 y = \pi^2/\sin \pi x = 1, \quad y(1/2), \quad y'(1/2) = \pi^2/2.$$

$$7.37. y'' + y = 2\operatorname{ctg} x, \quad y(\pi/2) = 1, \quad y'(\pi/2) = 2.$$

$$7.38. y'' + 16y = 16/\sin 4x, \quad y(\pi/8) = 3, \quad y'(\pi/8) = 2\pi.$$

$$7.39. y'' + y = 4\operatorname{ctg} x, \quad y(\pi/2) = 4, \quad y'(\pi/2) = 4.$$

$$7.40. y'' + y = 1/\sin x, \quad y(\pi/2) = 1, \quad y'(\pi/2) = \pi/2.$$